

# Nucleon structure functions at large- $x$



13th European Research Conference  
on Electromagnetic Interactions with Nucleons and Nuclei

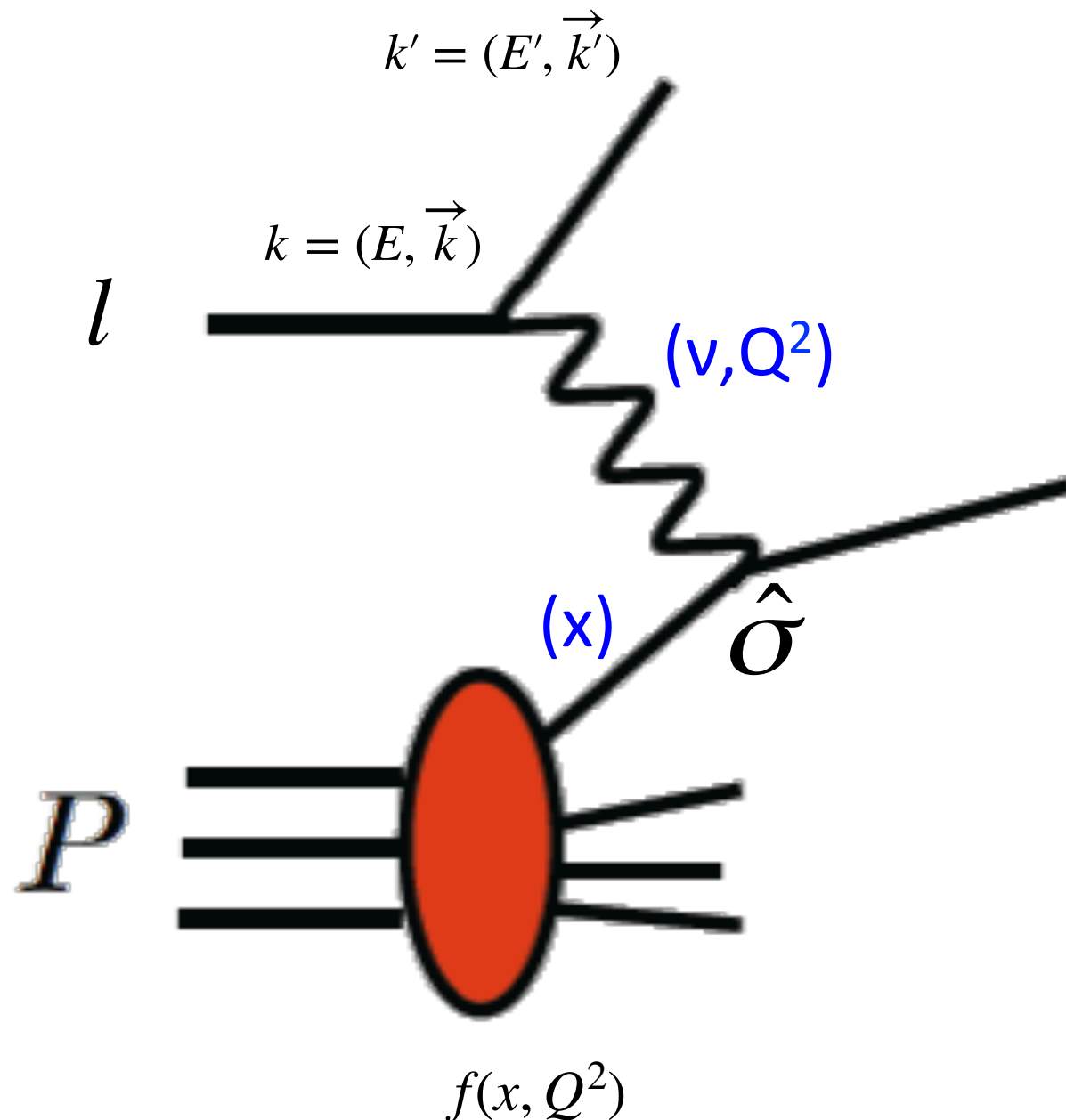
27 October – 02 November 2019

Paphos, Cyprus

Sanghwa Park  
(Stony Brook University)

# Deep Inelastic Scattering

microscope to see inside the hadron



**Brief recap of DIS kinematics**

$$Q^2 = -q^2$$

$$= -(k - k')^2$$

**Measure of resolution**

$$y = \frac{p \cdot q}{p \cdot k}$$

**Inelasticity**

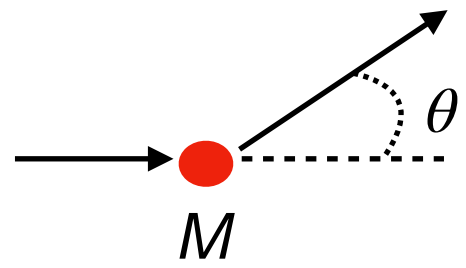
$$x = \frac{Q^2}{2p \cdot q}$$

**Momentum fraction carried by struck quark**

$$W^2 = (q + p)^2$$

**Inv. mass square of produced hadron**

# Deep Inelastic Scattering



$$\frac{d^2\sigma}{d\Omega dE'} = \frac{8\alpha^2 \cos^2(\theta/2)}{Q^4} \left[ \frac{F_2(x, Q^2)}{\nu} + \frac{2F_1(x, Q^2)}{M} \tan^2(\theta/2) \right]$$

$$R = \frac{\sigma_L}{\sigma_T} = \frac{F_2 M}{F_1 \nu} \left( 1 + \frac{\nu^2}{Q^2} \right) - 1$$

Two red arrows point from the  $\frac{F_2(x, Q^2)}{\nu}$  and  $\frac{2F_1(x, Q^2)}{M}$  terms in the first equation to the corresponding terms in the second equation.

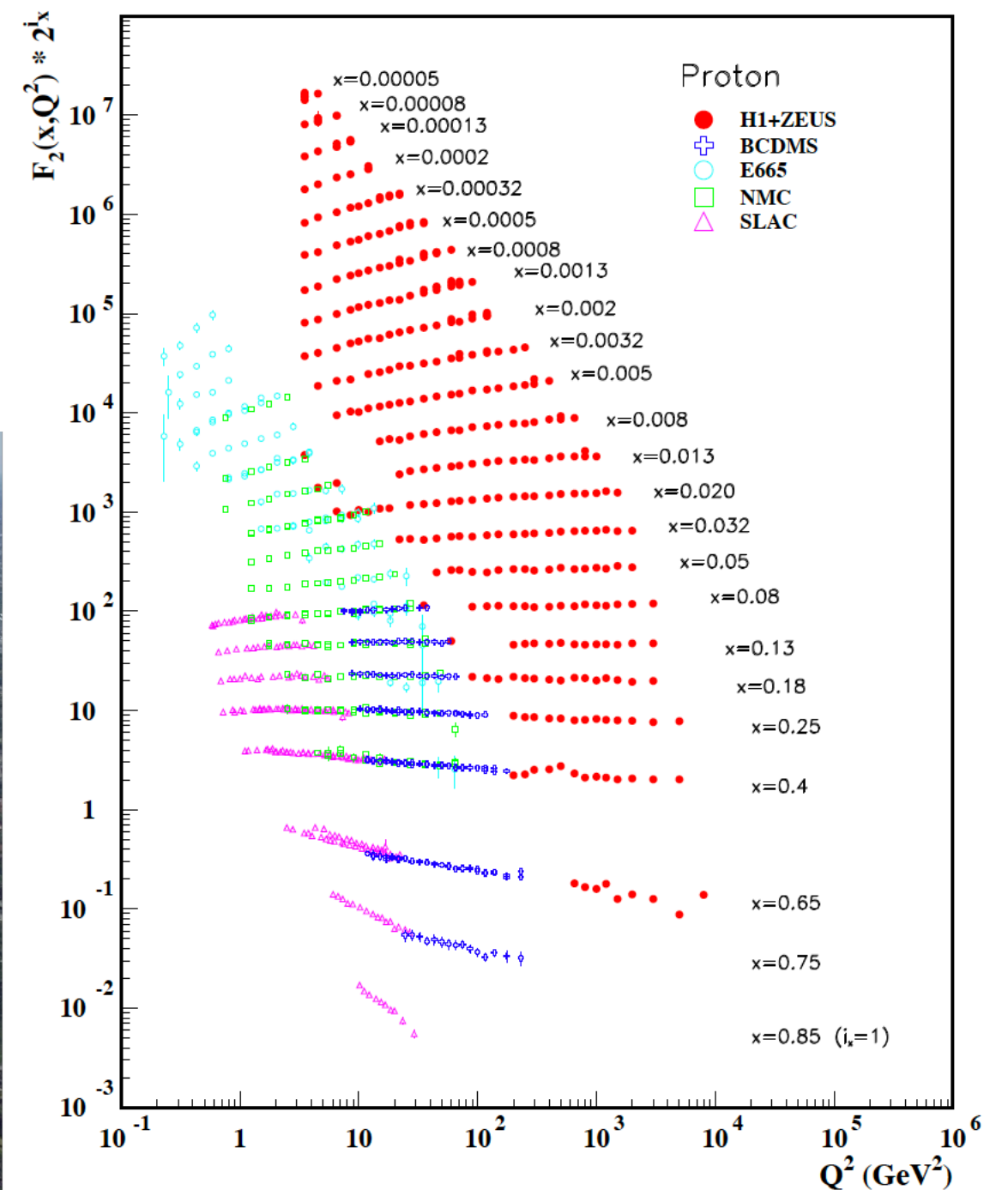
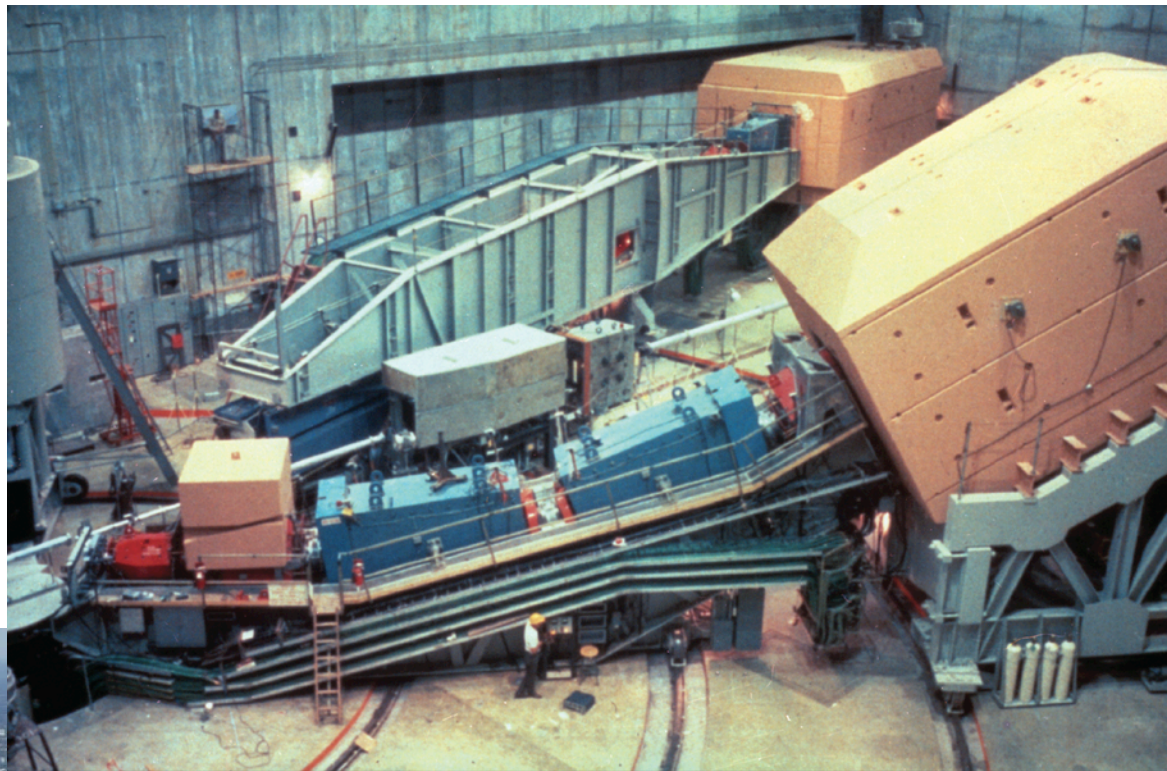
Information of internal structure of target nucleon

Directly related to parton distribution functions (PDFs)

In Quark parton model,  $F_1(x) = \frac{1}{2} \sum_i e_i^2 q_i(x, Q^2)$   $F_2(x, Q^2) = x \sum_i e_i^2 q_i(x, Q^2)$



# 50 years later...





# Large x PDFs

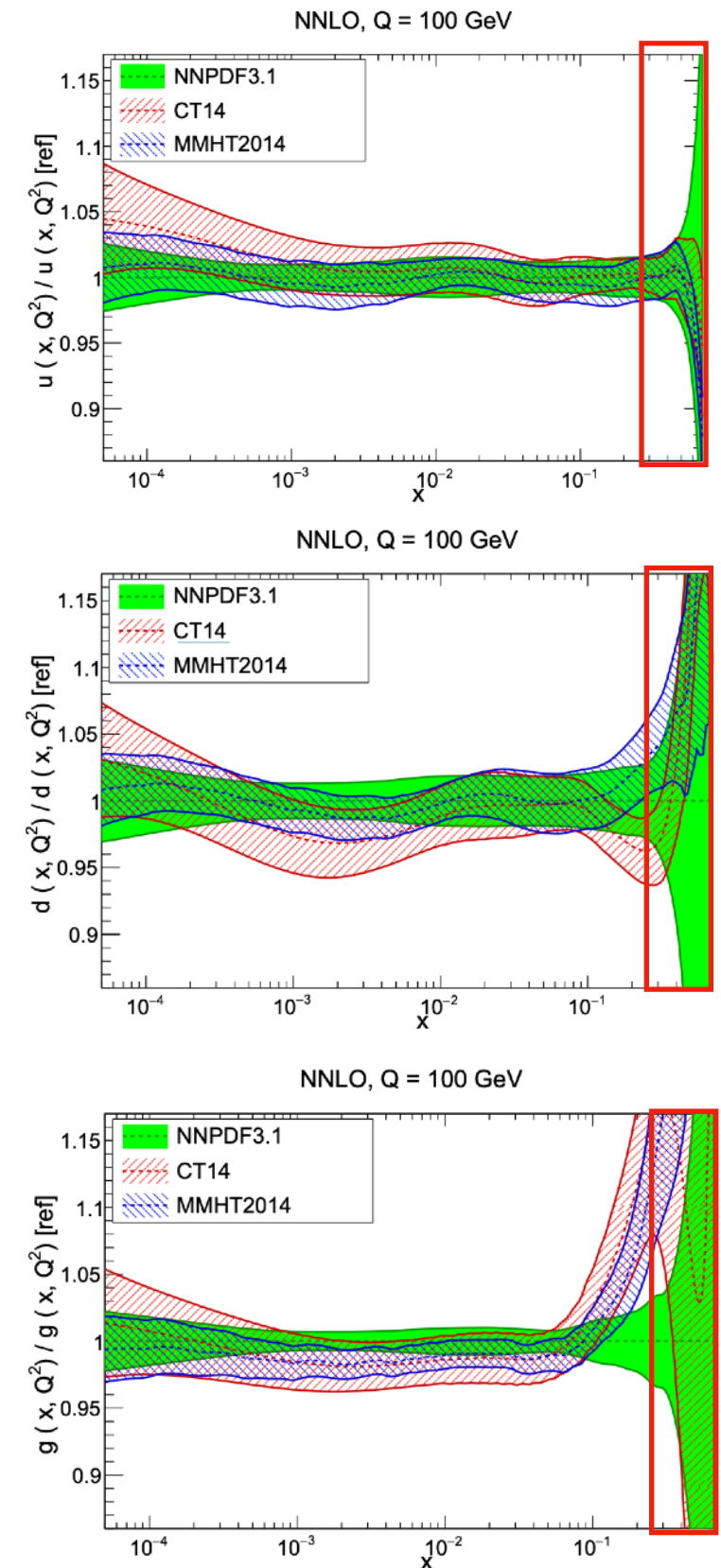
- Valence structure of hadron
- Improve constraints on PDFs at large-x

large x, low  $Q^2$

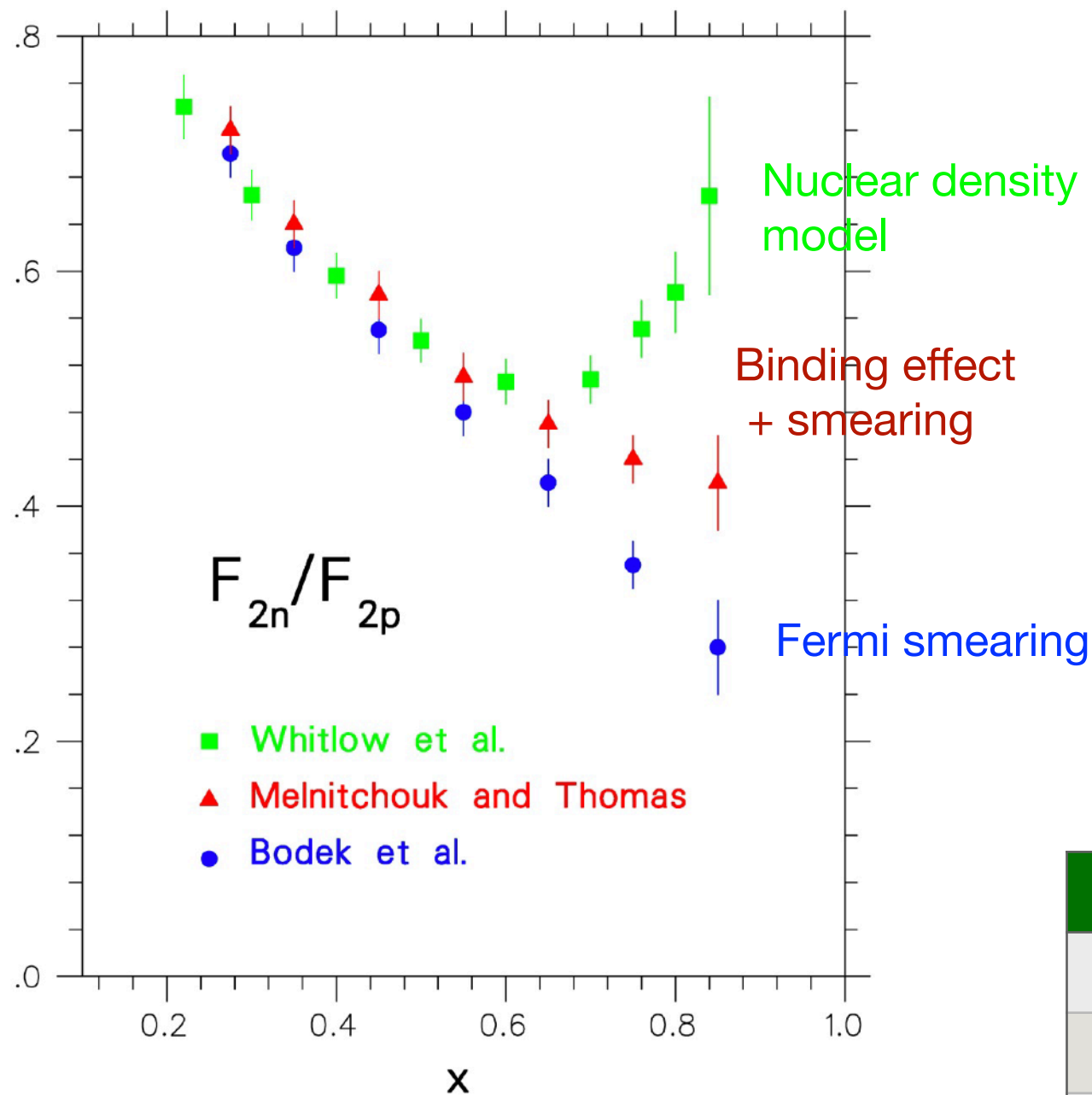
-> (evolution) low x, high  $Q^2$

Dominant systematic uncertainty source for precision cross sections and BSM search at LHC

- F2n/F2p ratio: d/u ratio at  $x \rightarrow 1$  limit
- Resonance structure of the hadron
- Quark-hadron duality



# Predictions for $F_2(n/p)$ , $d/u$ at $x \rightarrow 1$



$$F_2^p = x \left[ \frac{4}{9}(u + \bar{u}) + \frac{1}{9}(d + \bar{d}) + \frac{1}{9}(s + \bar{s}) \right]$$

$$F_2^n = x \left[ \frac{4}{9}(d + \bar{d}) + \frac{1}{9}(u + \bar{u}) + \frac{1}{9}(s + \bar{s}) \right]$$

At large  $x$ ,

$$\frac{F_2^n}{F_2^p} \approx \frac{1 + 4(d/u)}{4 + (d/u)}$$

Testing ground for hadron structure

	$F_2(n/p)$	$d/u$	$A_1(n)$	$A_1(p)$
SU(6)	2/3	1/2	0	5/9
Diquark model/Feynman	1/4	0	1	1
Quark model/Isgur	1/4	0	1	1
pQCD	3/7	1/5	1	1
QCD counting rules	3/7	1/5	1	1



$$F2(d) \neq F2(n) + F2(p)$$



No free neutron target exists

Deuteron is a weakly bound system

- chosen as effective neutron target

But,  $F2(d) \neq F2(n) + F2(p)$

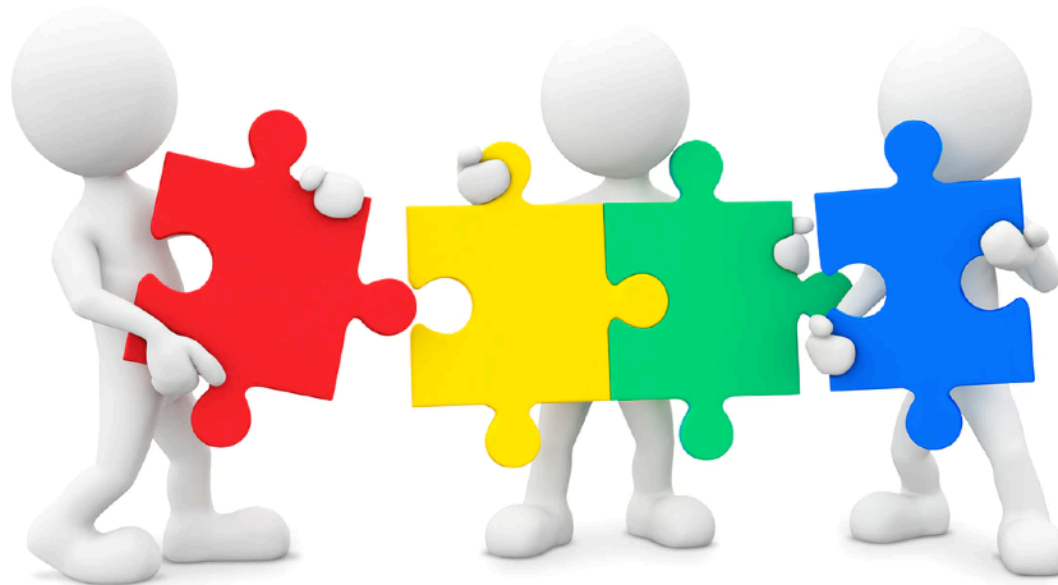
Large theory uncertainty from nuclear corrections

Binding and Fermi motion ->  
significant model dependence on  
Deuteron wave function

Off-shell corrections

Need more precise, preferably model-independent neutron target data!

# Recent progress



## A. Accardi (HiX2019)

### Large- $x$ treatment

	JLab & BONUS	HERMES	HERA I+II	Tevatron W,Z	LHC	$\nu$ +A di- $\mu$	Nucl. & offsh	HT TMC	Flex $d$	low-W DIS
<b>CJ15 *</b>	✓✓	✓	✓	✓	<i>in prog.</i>	✗	✓✓	✓	✓	✓
CT18			✓	✓ ✖✖	✓	✓			✓	
MMHT14			✖✖✖	✓ ✖✖	✓	✓	✓			
NNPDF3.1			✓		✓	✓		TMC only		
JR14	✓				✓	✓	✓	✓		
<b>ABMP16/AKP</b>				✓ ✖✖	✓	✓	✓/✓	✓	(✓)	✓
HERAPDF2.0			✓	✖						

## CTEQ-JLab (CJ)

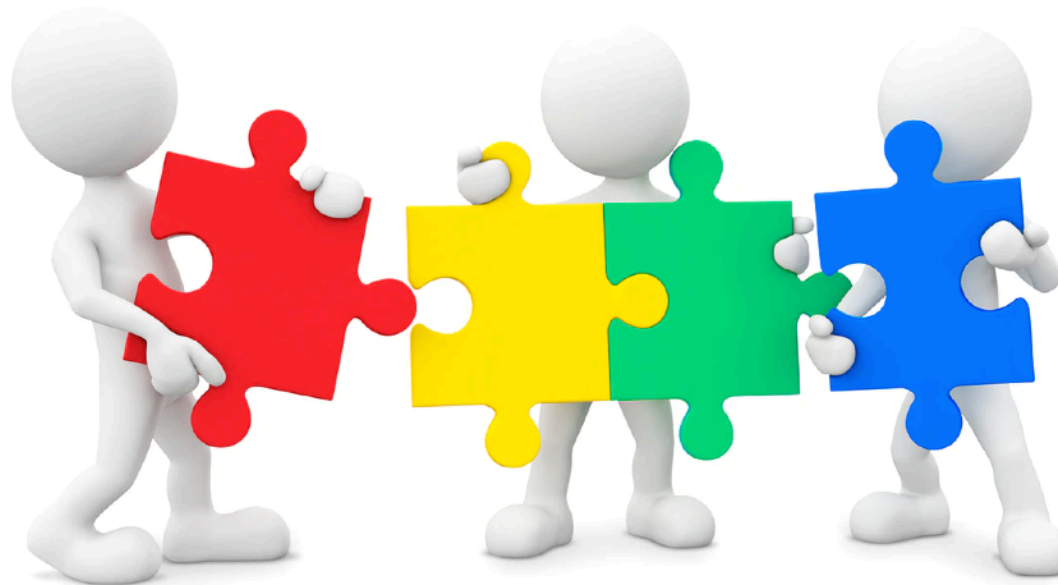
With focus on large  $x$ , low  $Q^2$   
Relaxing kinematic cuts to access larger  $x$

→ need to take into account subleading effects (target mass, higher twist, ..)

Including new fixed target data and LHC, Tevatron



# Recent progress



## News from JLab

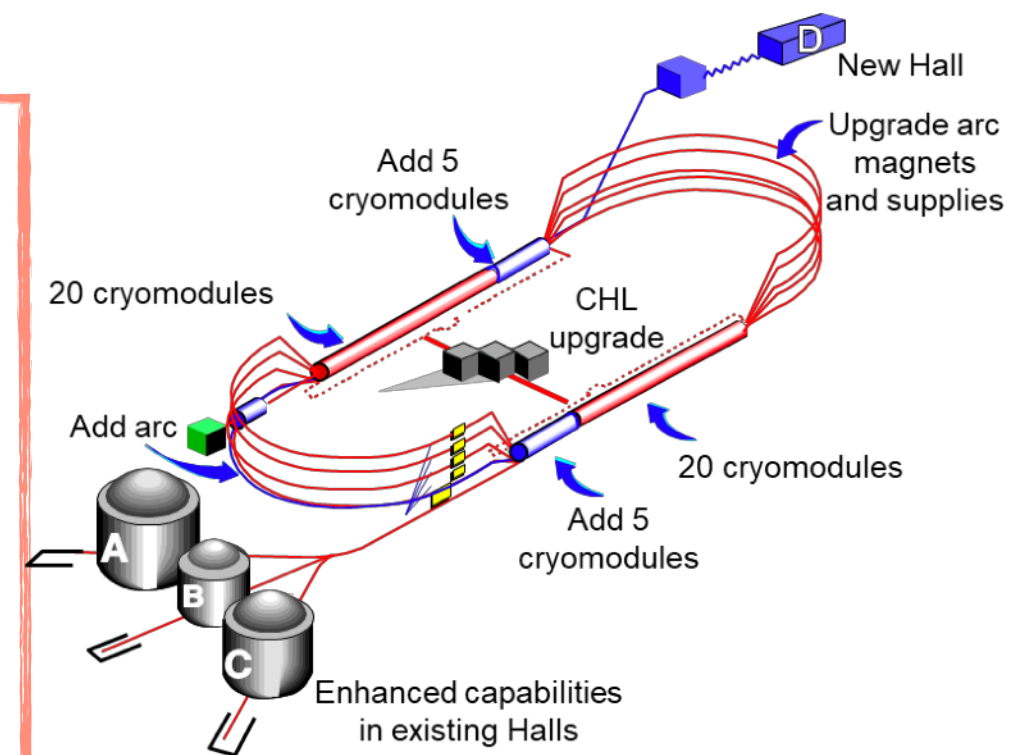
Precision F2 data at large  $x$ , low  $Q^2$

Less model dependent F2n/F2p

- A=3 mirror nuclei
- Spectator tagging

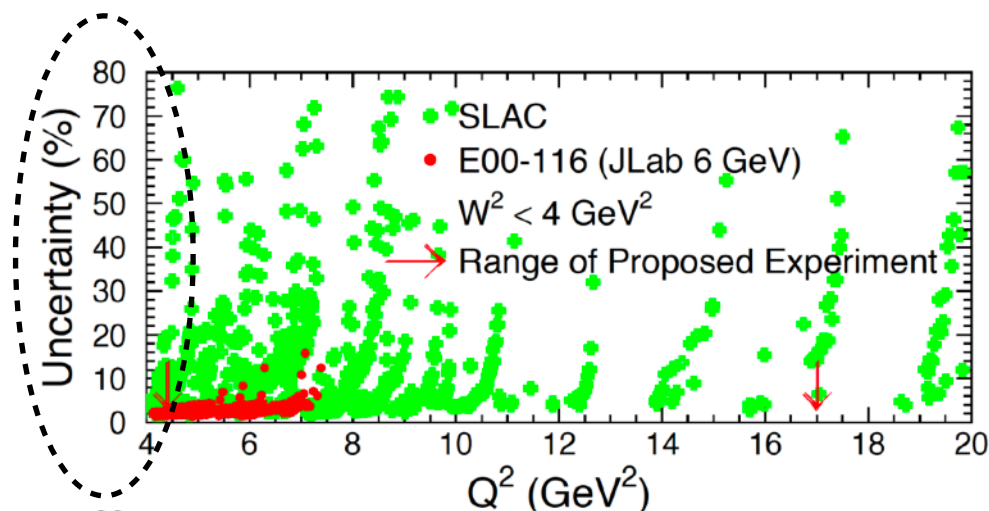
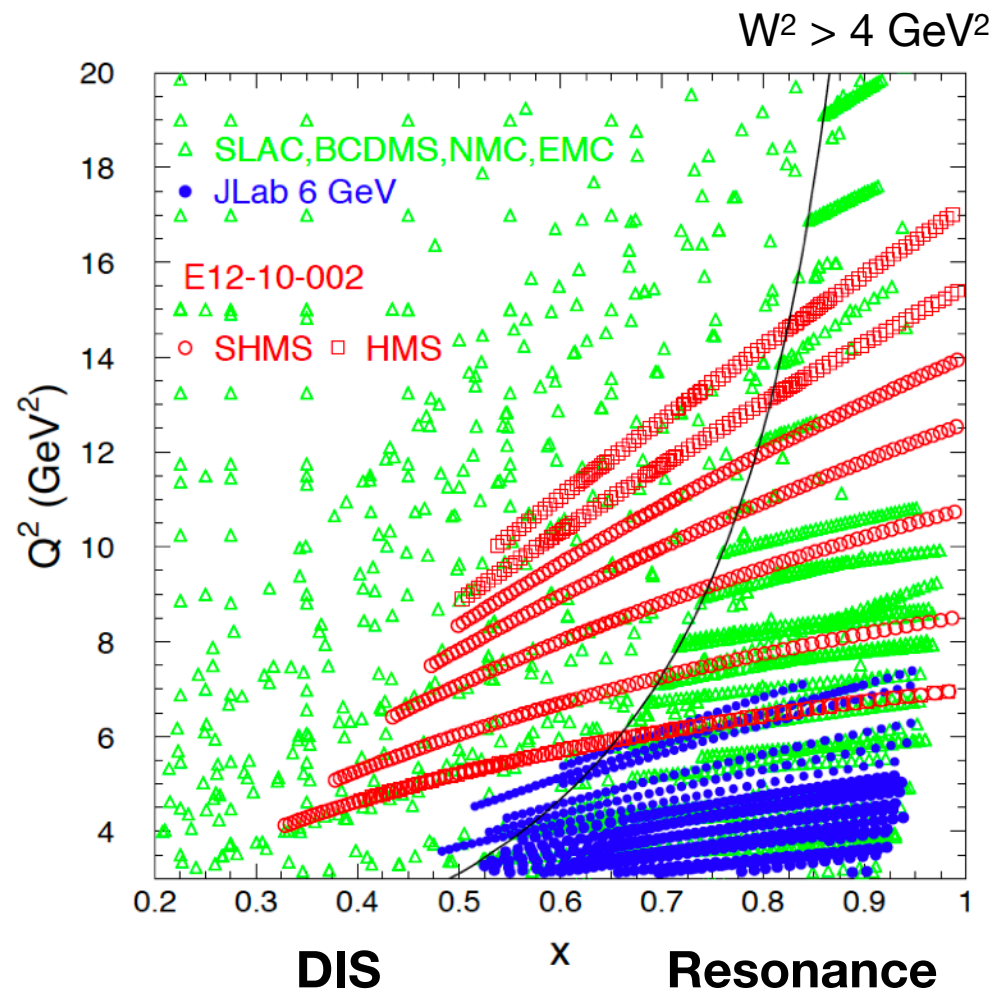
Model independent approach - SoLID PVDIS

And, W asymmetry (FNAL, LHC, RHIC) puts strong constraints on d quark



**Successfully completed  
12 GeV upgrade in 2017**

# Precision $F_2$ measurement at large $x$



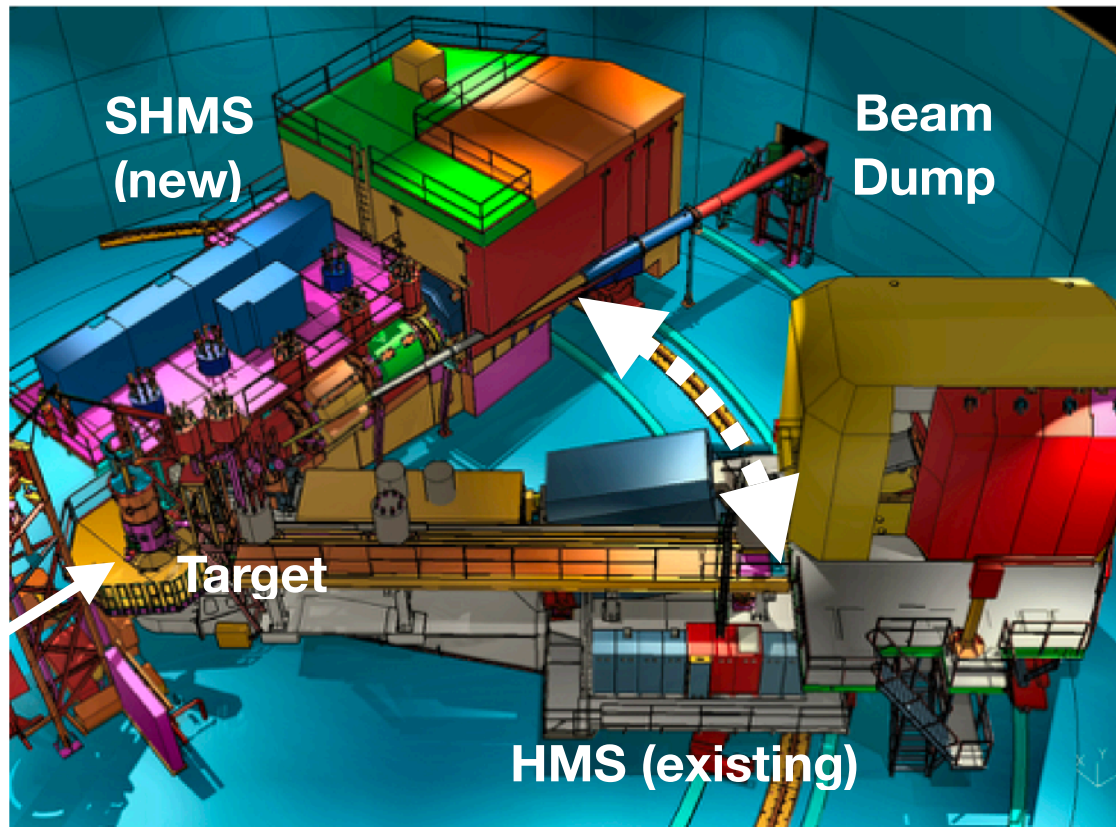
- SLAC data - limited statistics, mostly low  $Q^2$   
 -> JLab 12 GeV can extend  $Q^2$  coverage with high precision
- Inclusive  $H(e,e')$  and  $D(e,e')$  measurements at Hall C
- New data taken in 2018 - extended  $x$  and  $Q^2$  coverage
- Extend quark-hadron duality studies from 6 GeV experiment (E00-116)

S.P. Malace *et al.*, Phys. Rev. C 80 035207 (2009)

S.P. Malace *et al.*, Phys.Rev.Lett. 104 (2010) 102001



## Hall C High Momentum Spectrometers

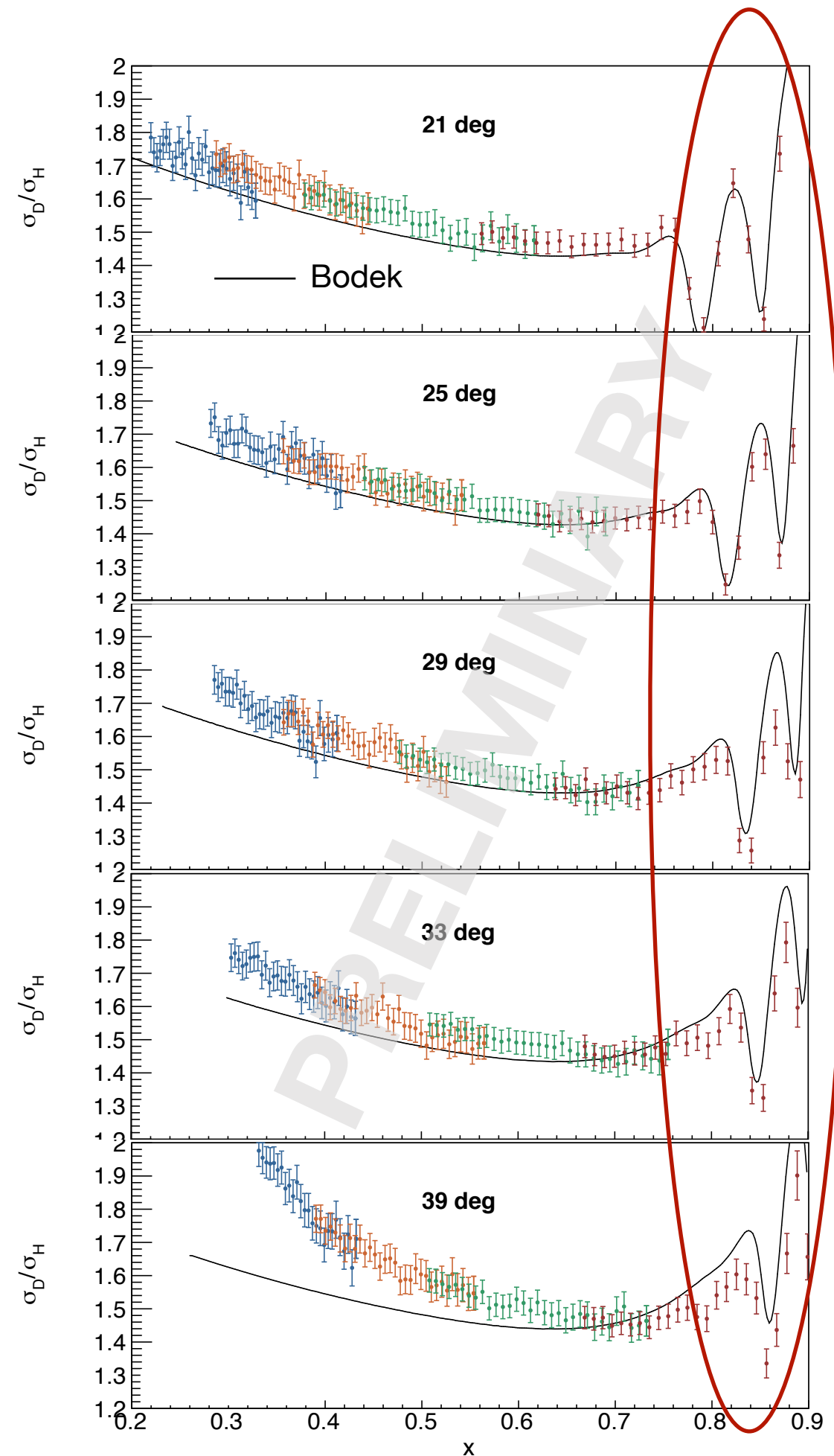


Inclusive D/H cross section ratio from new Hall C data (LH2 and LD2 targets)

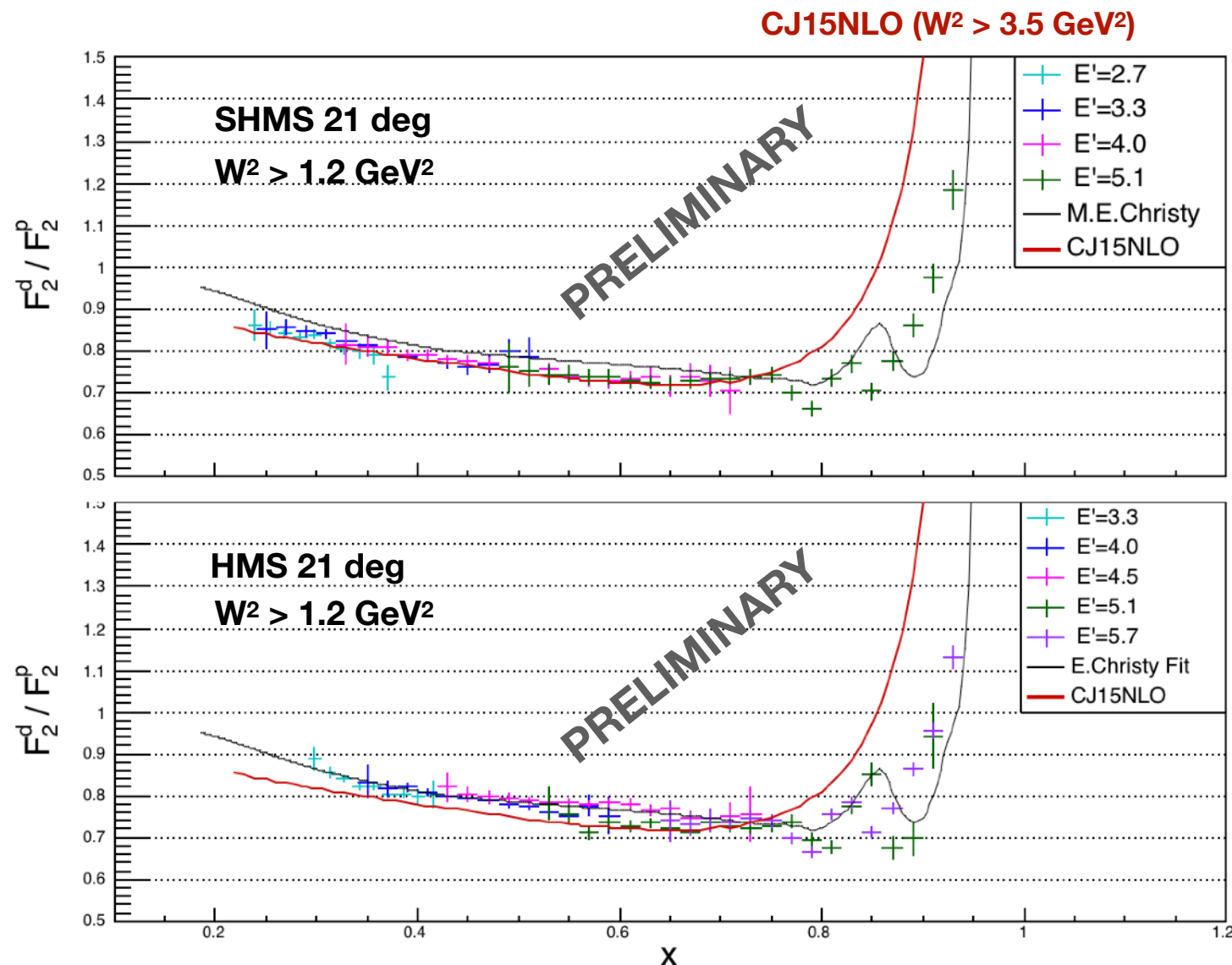
Preliminary results shown charge symmetry background, residual pion contamination not taken into account

Resonance structure shown at large- $x$  region

Higher Q<sup>2</sup> reach



# $F_2^d/F_2^p$ Ratio



(\* Statistical uncertainty only)

**Very first look of structure function ratio**

**Assume  $R_d = R_p$**   $\frac{\sigma^d}{\sigma^p} \approx \frac{F_2^d}{F_2^p}$

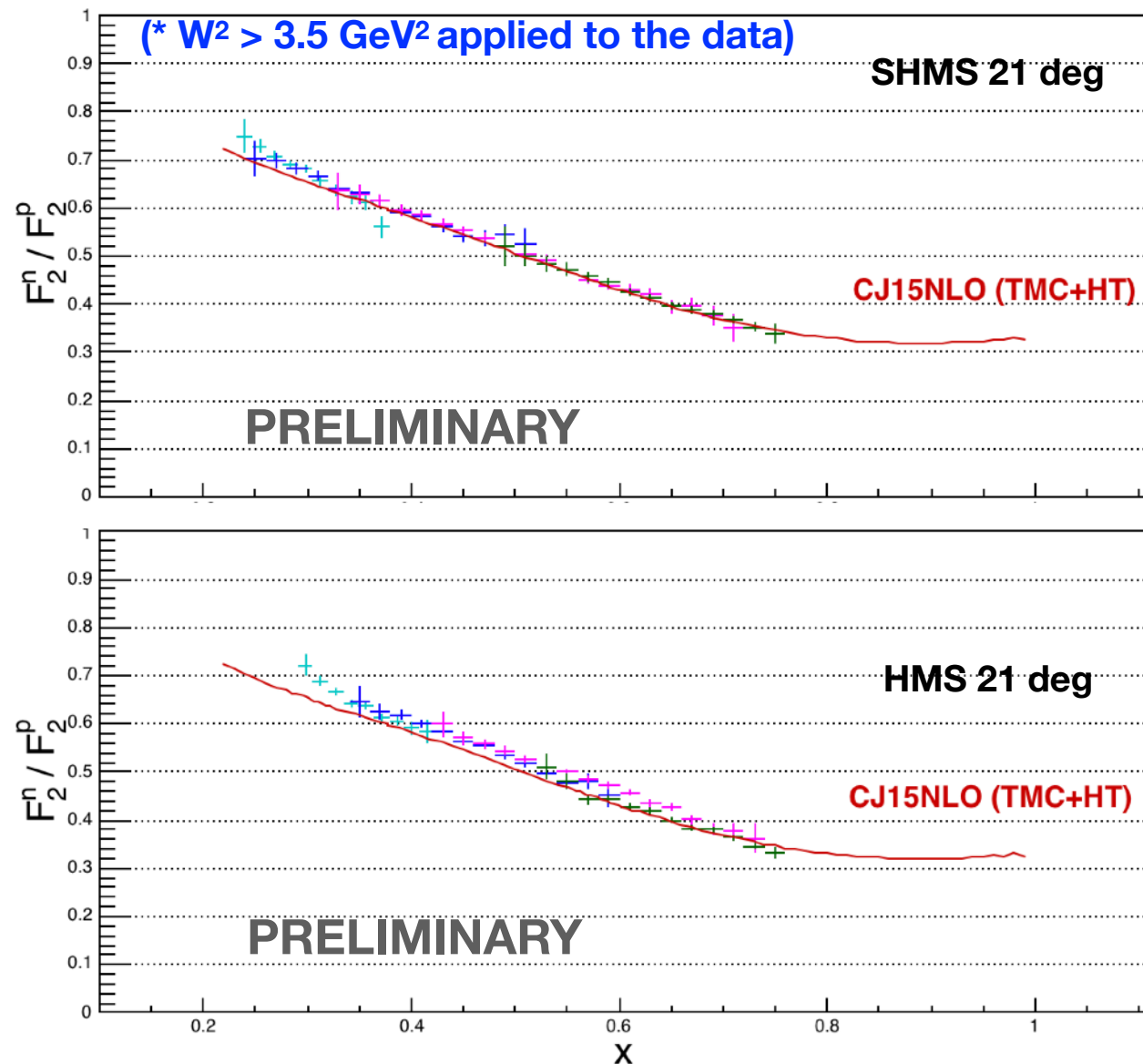
**Only small subset of data shown here**

**M.E. Christy and P.E. Bosted fit:**  
**Phys. Rev. C 81, 055213 (2010)**  
**includes resonance data**

**CJ15NLO:**  
<https://www.jlab.org/theory/cj/>  
**DIS only**



# $F_2^n/F_2^p$ Ratio



## $F_2^n/F_2^p$ using CJ15NLO $F_2$ ratio

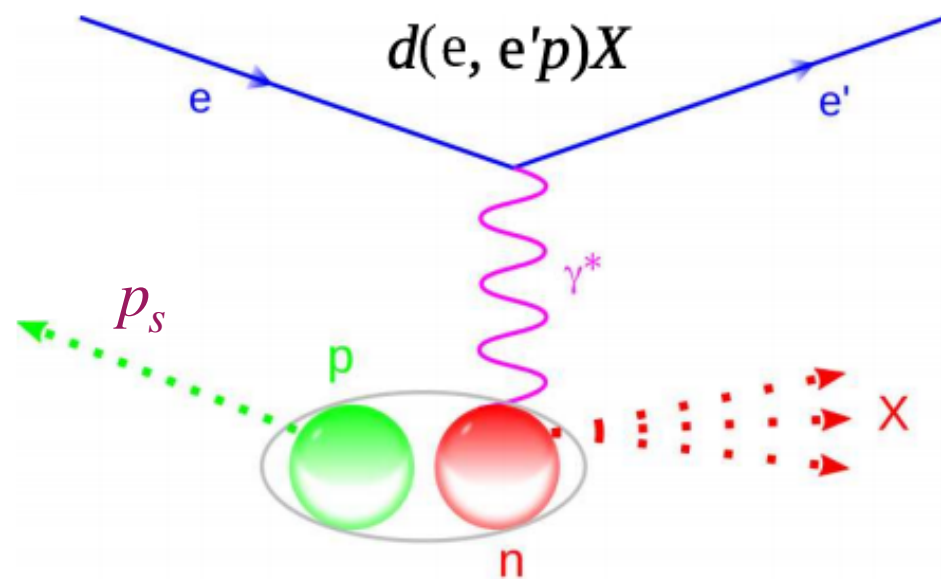
$$\left(\frac{F_2^d}{F_2^p}\right)_{Data} \times \left(\frac{F_2^n}{F_2^p}\right)_{CJ} / \left(\frac{F_2^d}{F_2^p}\right)_{CJ}$$

- CJ PDF extraction includes state-of-the-art deuteron nuclear corrections (smearing, off-shell, ..)
- Multiply  $F_2^d/F_2^p$  from data by  $F_2^n/F_2^d$  from CJ to extract  $F_2^n/F_2^p$  ratio
- Can be compared with MARATHON  $F_2^n/F_2^p$  from  $3\text{H}/3\text{He}$  ratio data

\*Statistical uncertainty only. Theory uncertainties not included

# BoNus: Spectator tagging

Barely Off-shell Nucleon Structure experiment (@ Hall B)



Tagging spectator protons in coincidence with the scattered electrons

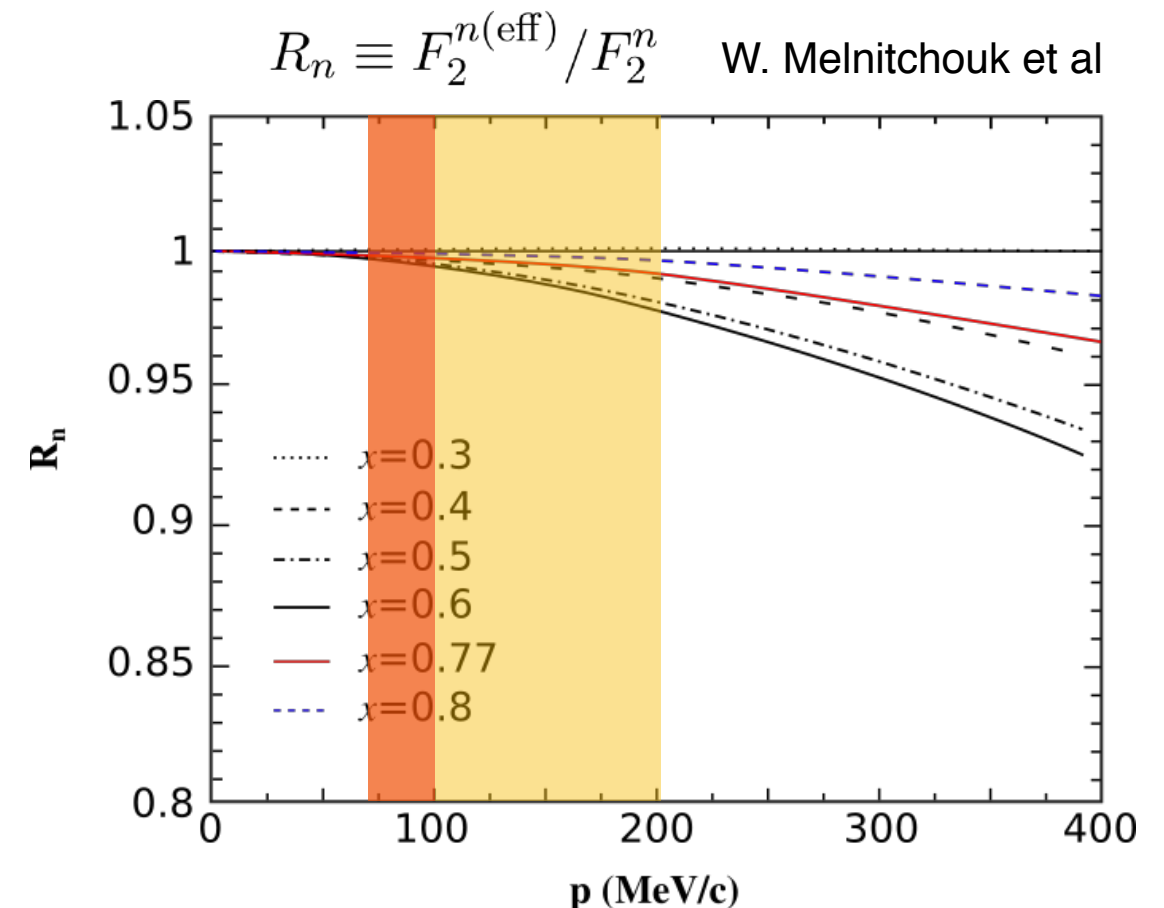
$$e + d \rightarrow e' + p_s + X$$

**Proton with small momentum in the backward hemisphere**

$$p_s \leq 100 \text{ MeV}$$

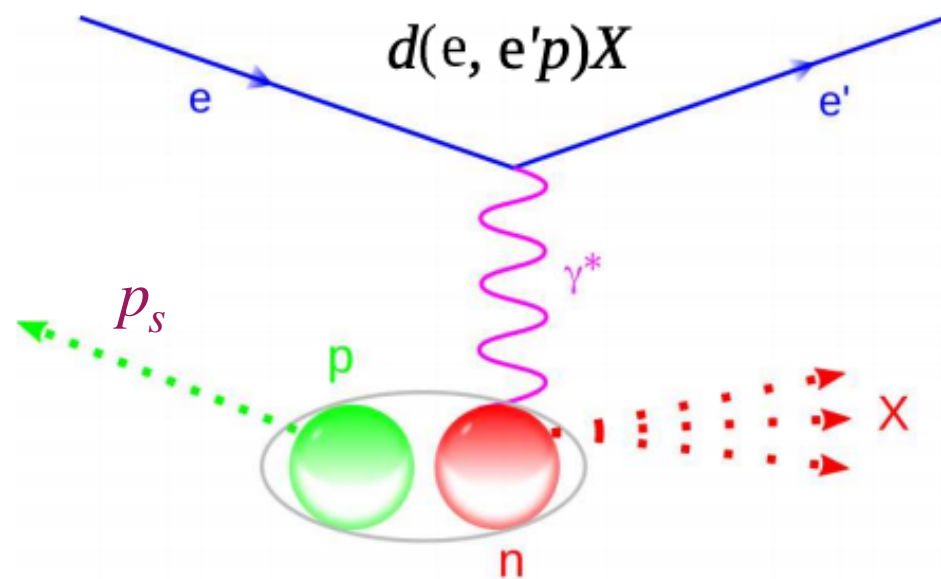
$$\theta_{pq} \geq 100$$

→ minimize probability of rescattering of spectator proton with hadronic debris



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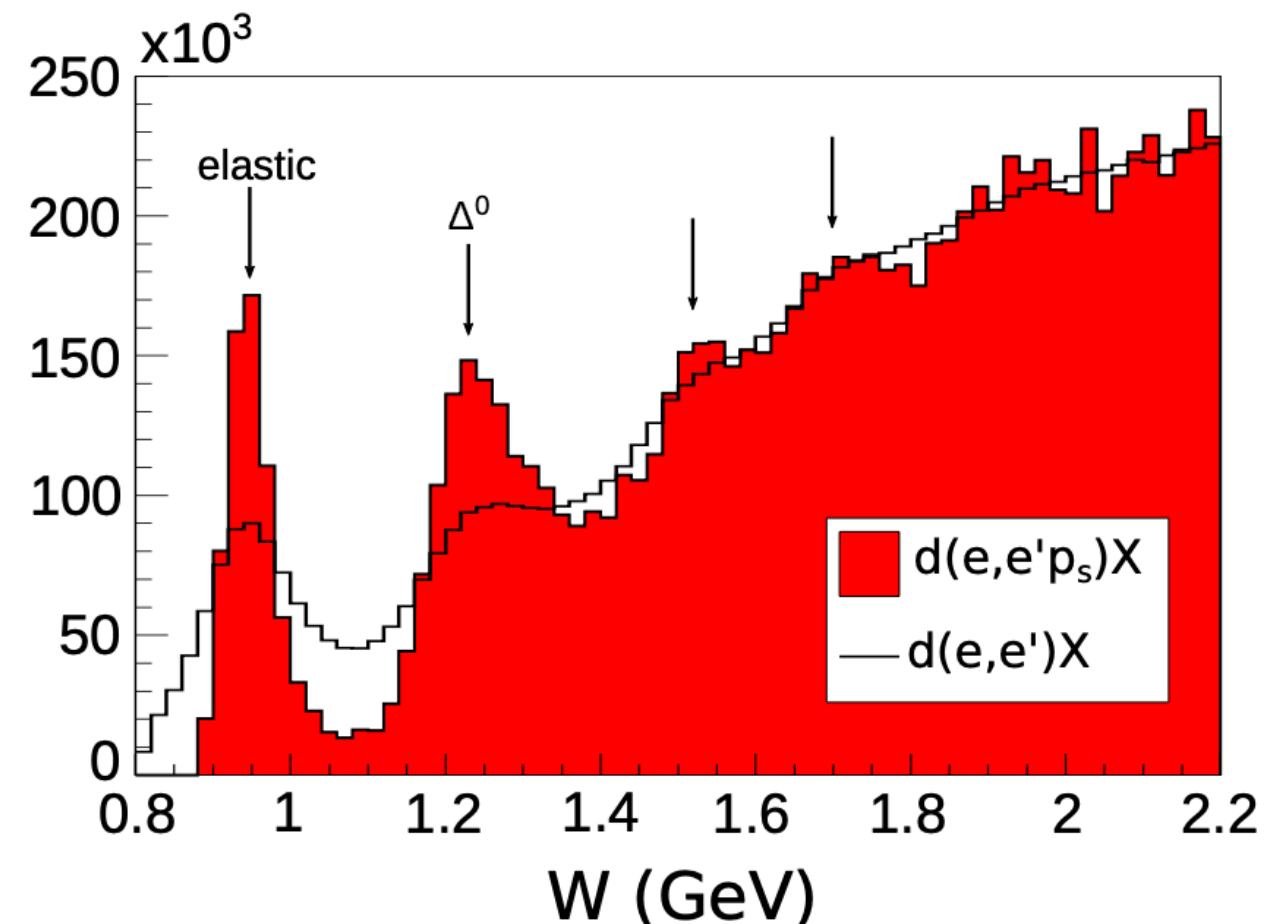
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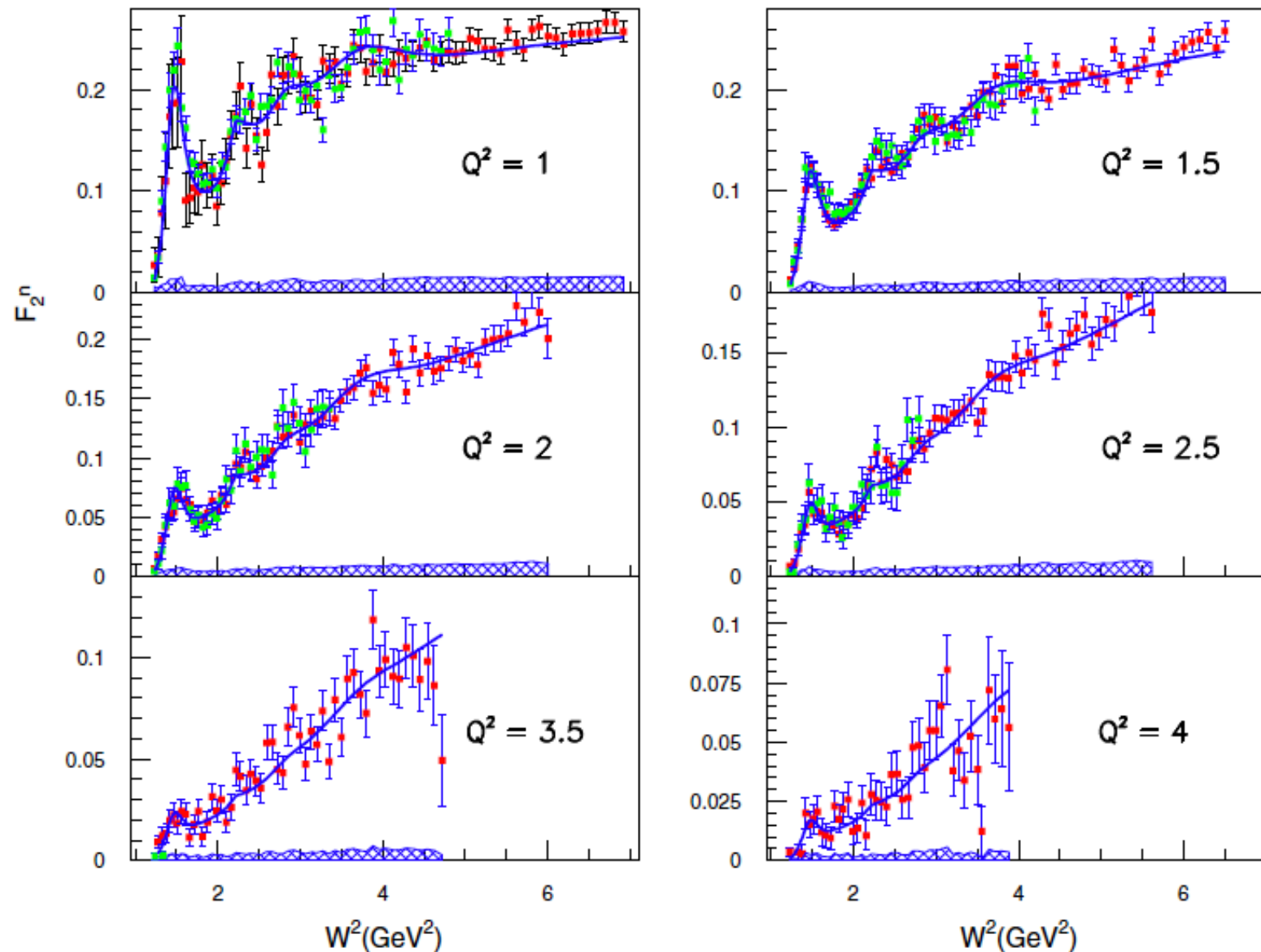
→ minimize probability of rescattering of spectator proton with hadronic debris





# BoNus results

S. Tkachenko et al., Phys. Rev. C 89, 045206 (2014)

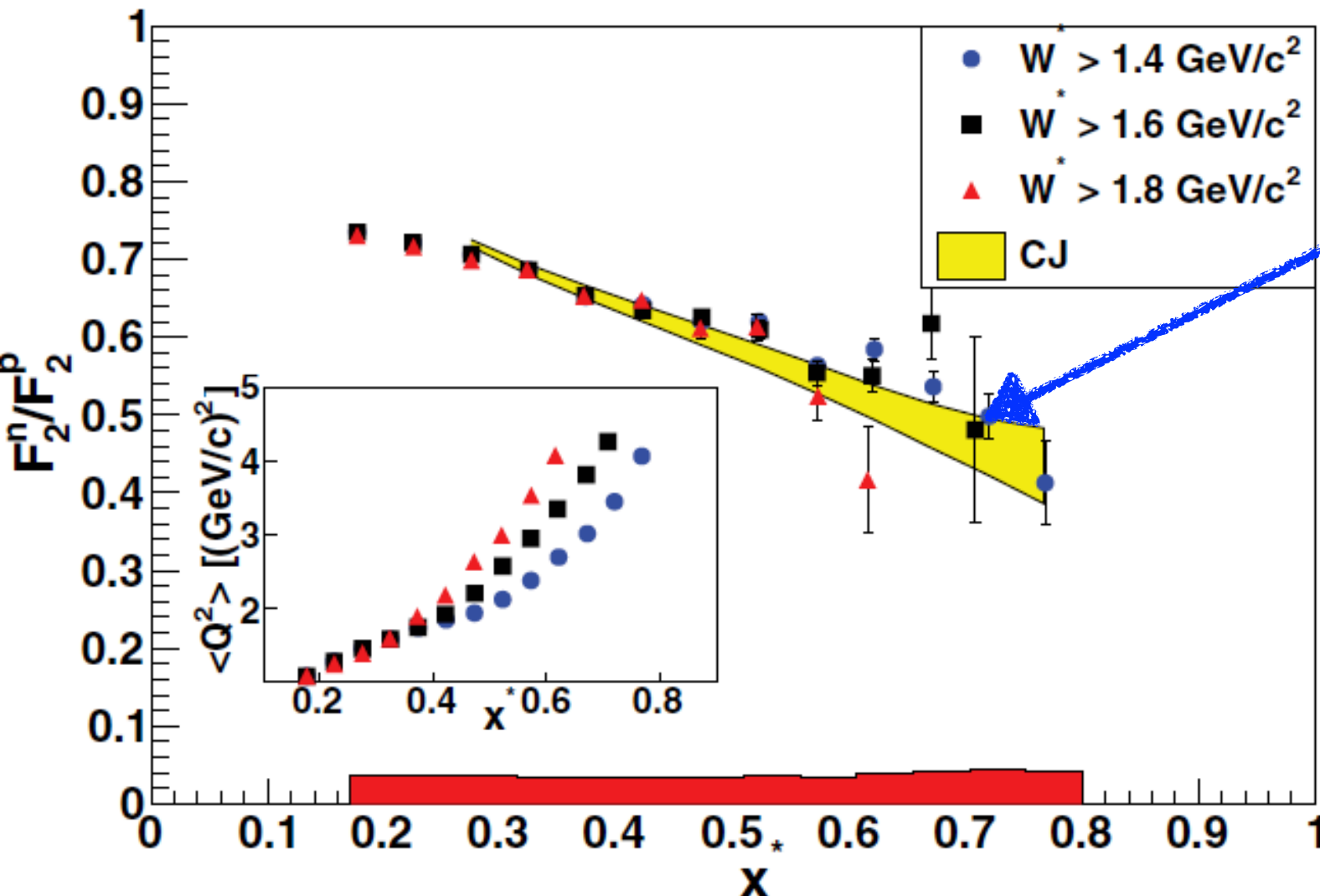


Extracted (nearly) free neutron structure function using  $F_2^d$  from inclusive deuteron and proton data fit (M. Christy and P. Bosted)

Study local quark-hadron duality of neutron (I.N et al PRC91 (2015) 055206)

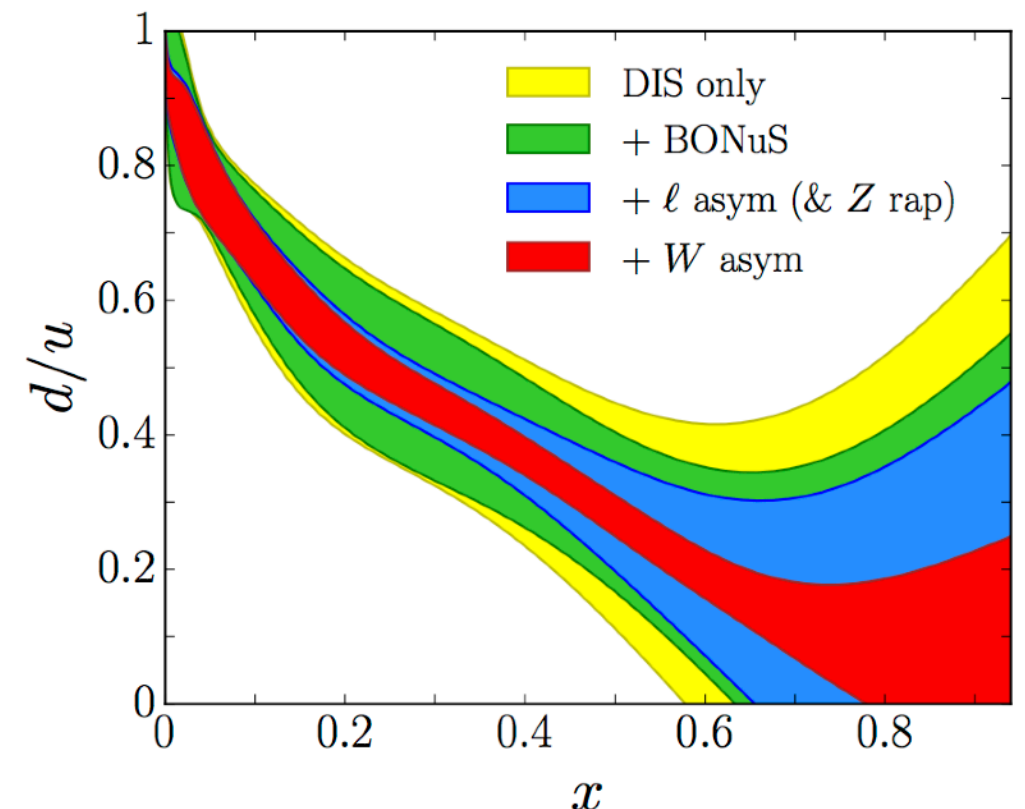
# BoNus results

S. Tkachenko et al., Phys. Rev. C 89, 045206 (2014)



Relaxing  $W$  cut add statistical power, but also start showing resonance structure

Impact of BoNus data  
-> Included to CJ15



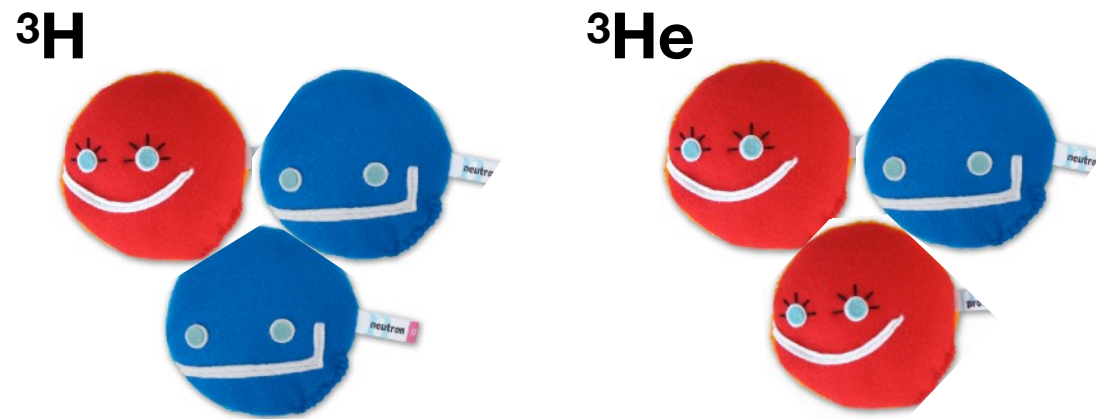
Successor experiment BoNus12 schedule to run 2020  
Extends kinematic coverage:

$0.1 < x < 0.8$ ,  $Q^2$  of 1-14  $\text{GeV}^2$ ,  $W$  up to 4 GeV

Also, at EIC! (EPJ Web Conf. 112 (2016) 01022)

# 3H/3He DIS - MARATHON @Hall A

A=3 mirror nuclei



Form EMC-type ratios

$$R(^3\text{He}) = \frac{F_2^{^3\text{He}}}{2F_2^p + F_2^n} \quad R(^3\text{H}) = \frac{F_2^{^3\text{H}}}{F_2^p + 2F_2^n}$$

Super ratio  $R^* = \frac{R(^3\text{He})}{R(^3\text{H})}$

Now depends on relative difference in nuclear effects

Differences in the nuclear effects small,  $R^* \approx 1$  (theory calculations)

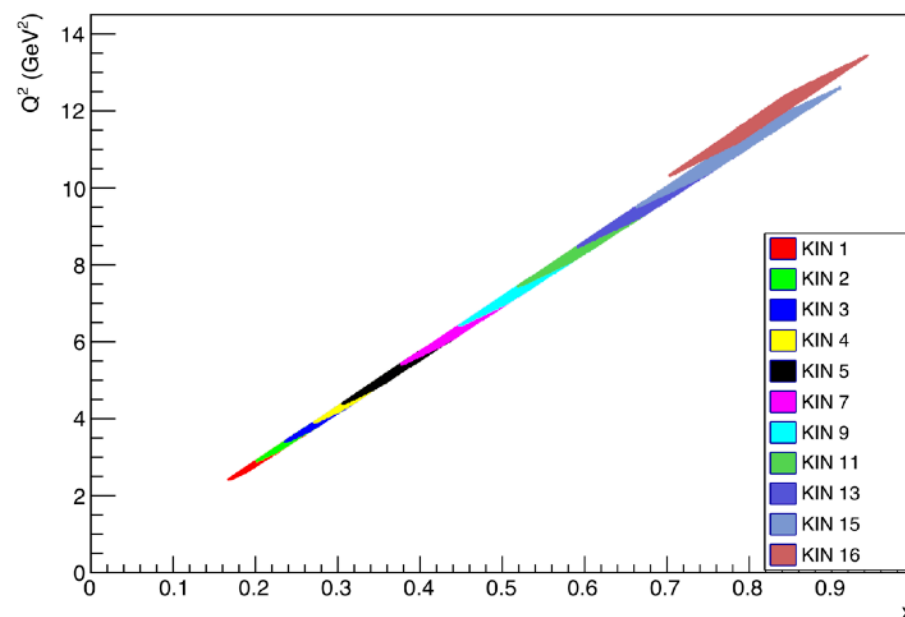
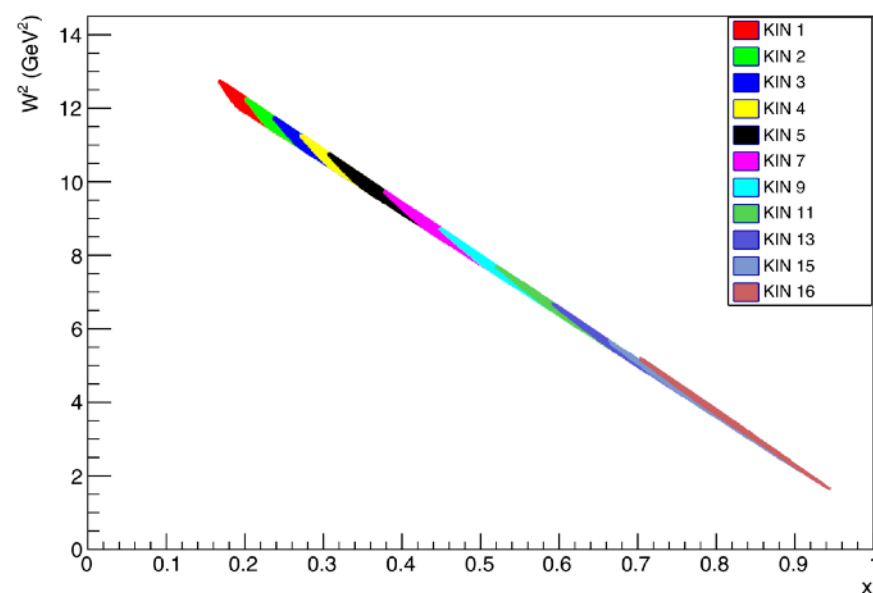
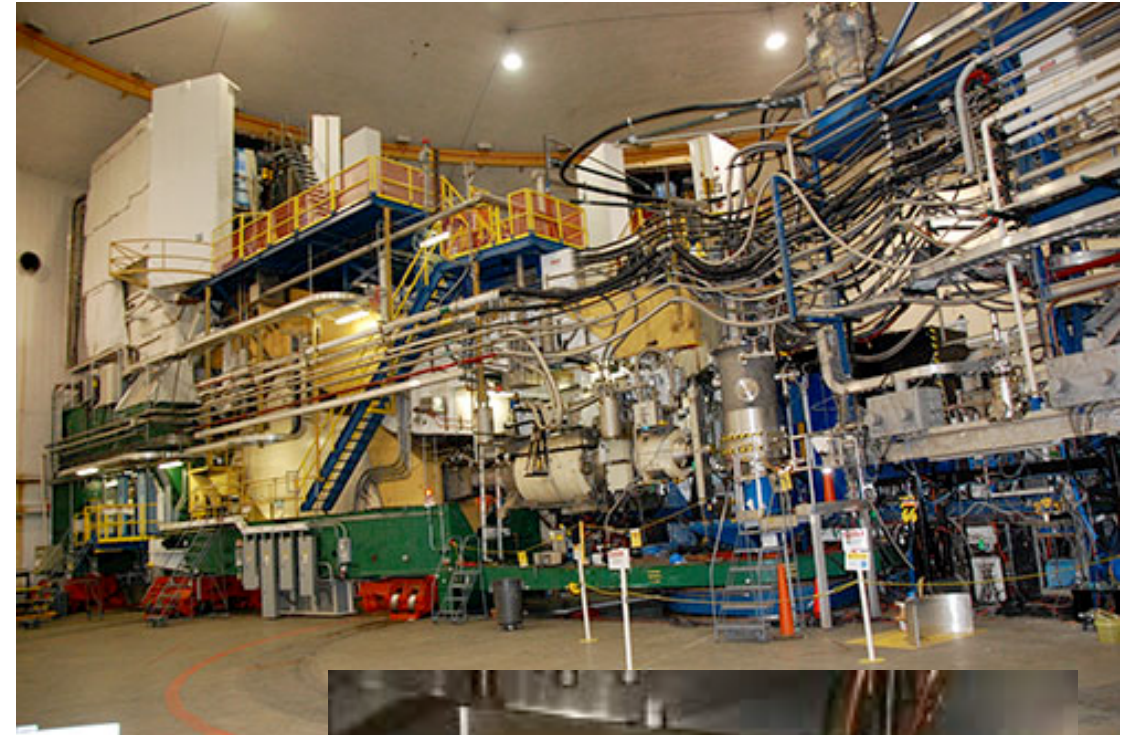
$$\frac{\sigma^{^3\text{He}}}{\sigma^{^3\text{H}}} = \frac{F_2^{^3\text{He}}}{F_2^{^3\text{H}}} = R^* \frac{2F_2^p + F_2^n}{F_2^p + 2F_2^n}$$

$$\frac{F_2^n}{F_2^p} = \frac{2R^* - \sigma^{^3\text{He}}/\sigma^{^3\text{H}}}{2\sigma^{^3\text{He}}/\sigma^{^3\text{H}} - R^*}$$

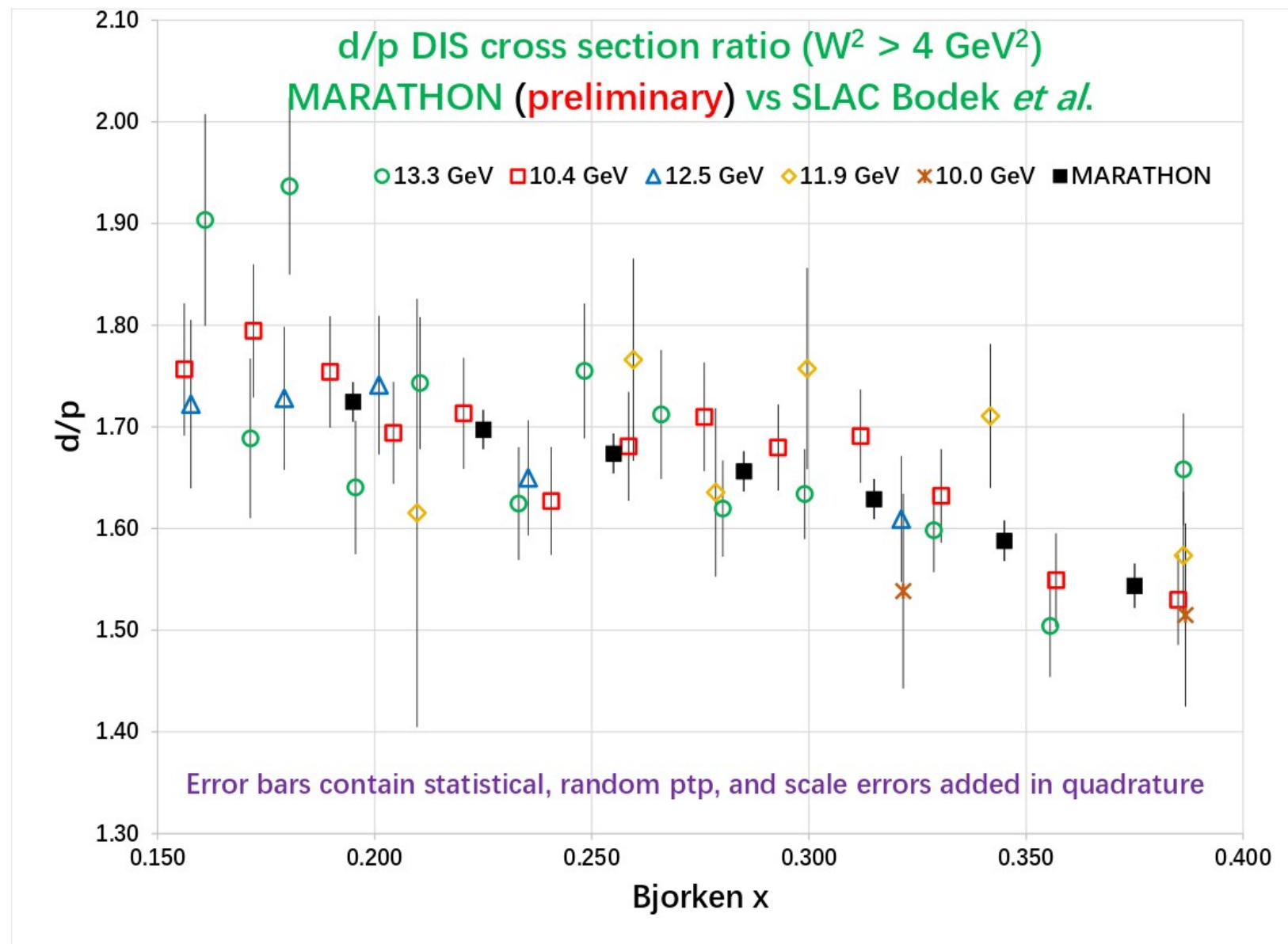


# MARATHON experiment

- 10.6 GeV beam, fixed scattered electron momentum (3.1 and 2.9 GeV), scattering angle 17-36 deg
- 3H, 3He, 2H, 1H targets
- Also measure EMC effects in 3He and 3H (first experimental data) and others



# d/p DIS cross section ratio

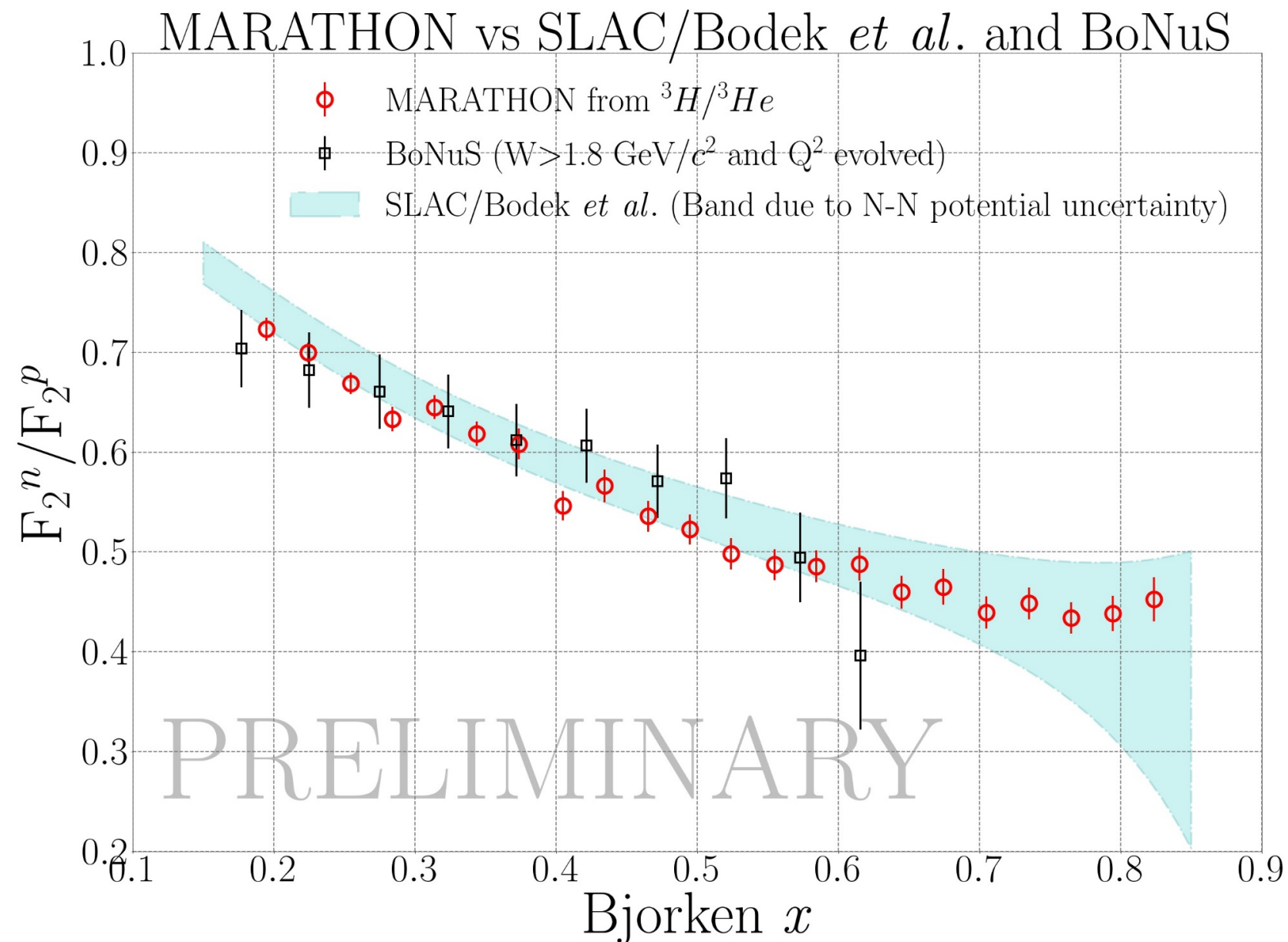


d/p cross section ratio measured at relatively low x with high precision

In excellent agreement with SLAC data

Used to normalize  $F_2(n/p)$  ratio from  $3\text{H}/3\text{He}$  data

# F2 ratio from 3H/3He



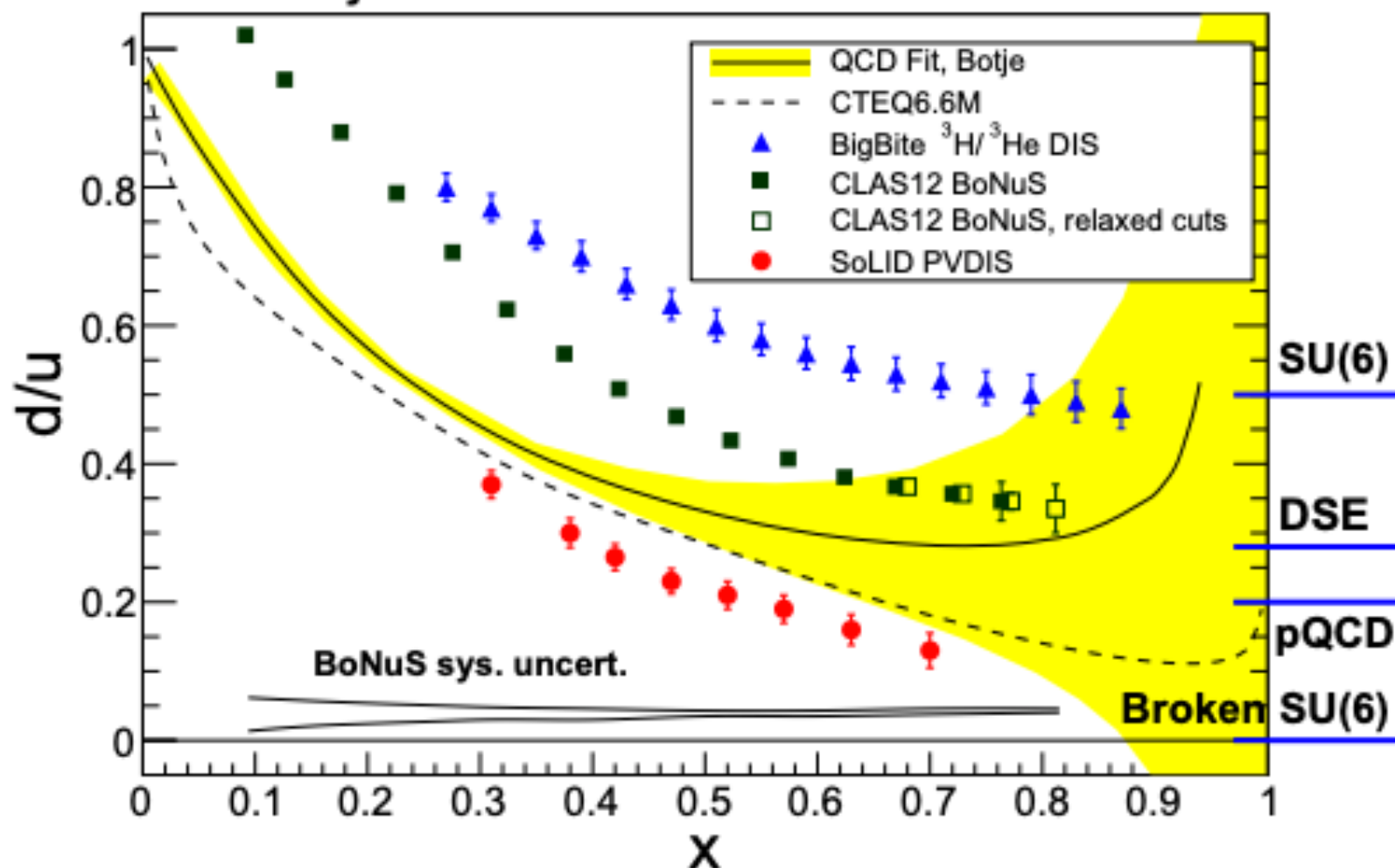
F2 neutron to proton ratio from 3H and 3He cross section ratio +  $R^*$  from Kulagin and Petti model

$x_{\text{max}}$  reaches to  $\sim 0.83$ , analysis in progress towards publication



# Constraints on d/u from JLab 12GeV

Projected 12 GeV d/u Extractions



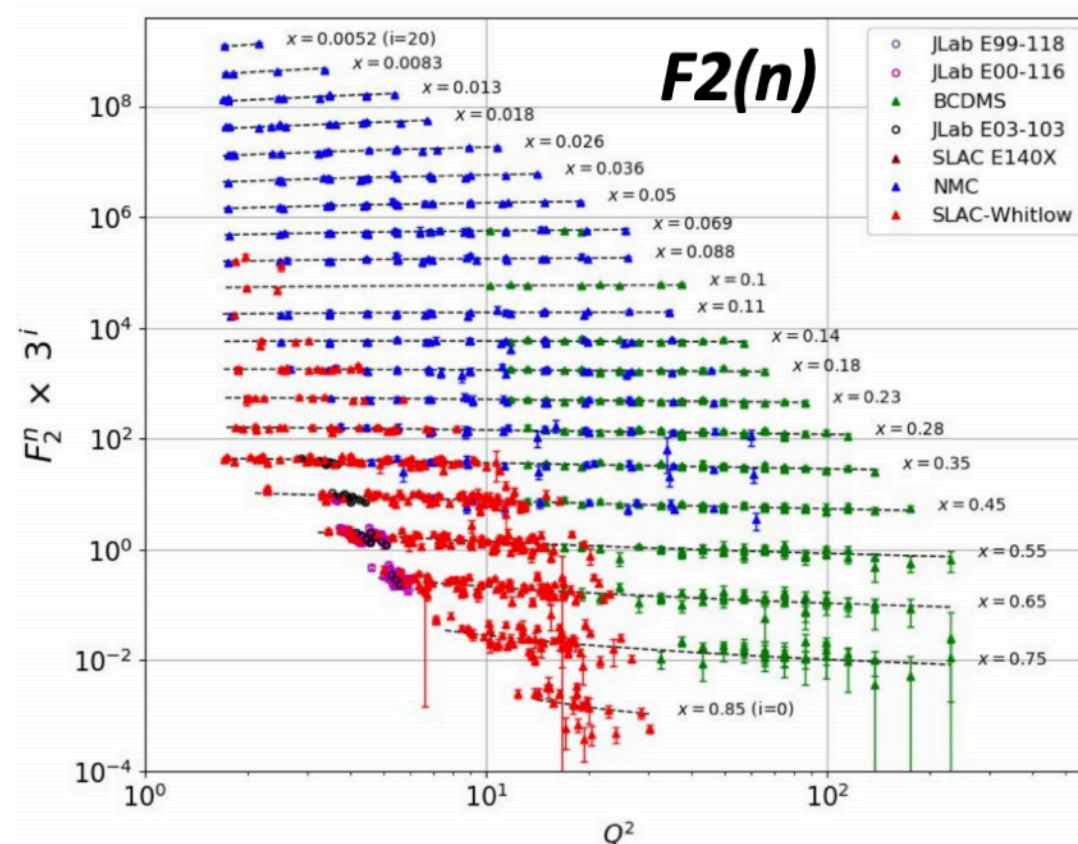
- Model dependent approach:  
Traditional Inclusive  
Measurements with deuterium
- Less model dependent approaches:  
**3H/3He ratio (MARATHON) - took data in 2018!**  
**Spectator tagging (BoNus12) - will run in 2020**
- Model independent approach:  
**PVDIS on proton (SoLID)**

Talk by K. Kumar (Parity violation program at Jefferson Lab)

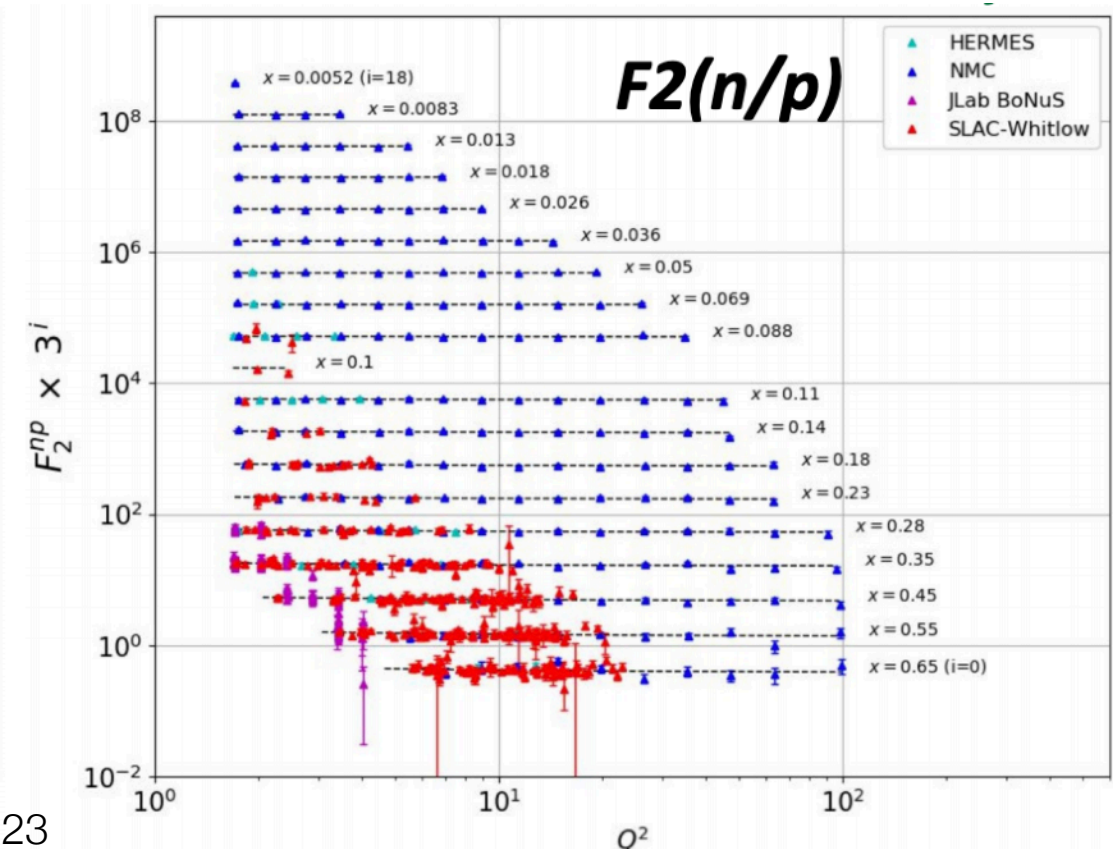
# Database of neutron $F_2$

S. Li (Univ. New Hampshire) + CJ

- $F_2^n$  extraction from world DIS data
- Unpolarized proton and deuterium DIS data ( $F_2$  and ratios) + nuclear corrections from global QCD analysis  $\rightarrow F_2$  neutron
- Extract  $F_2^n, F_2^p, F_2(n/p)$ , nonsinglet moment

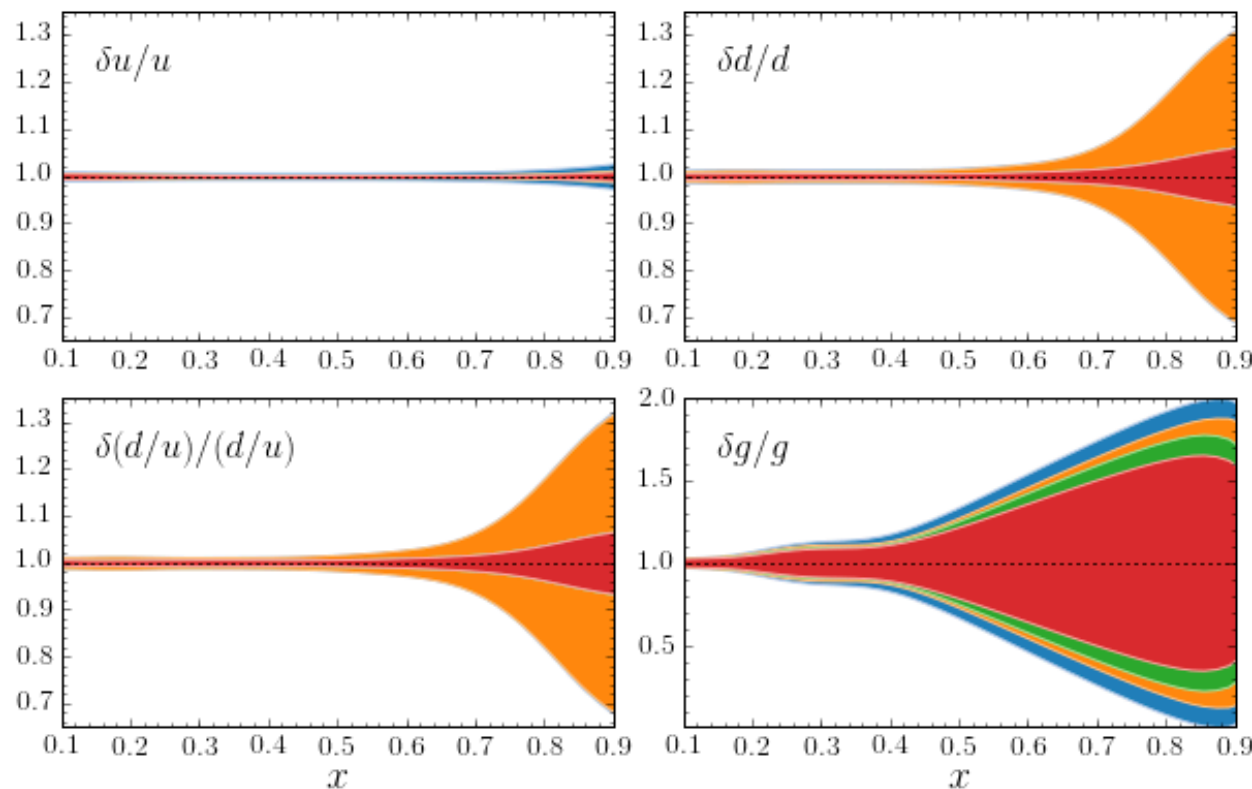
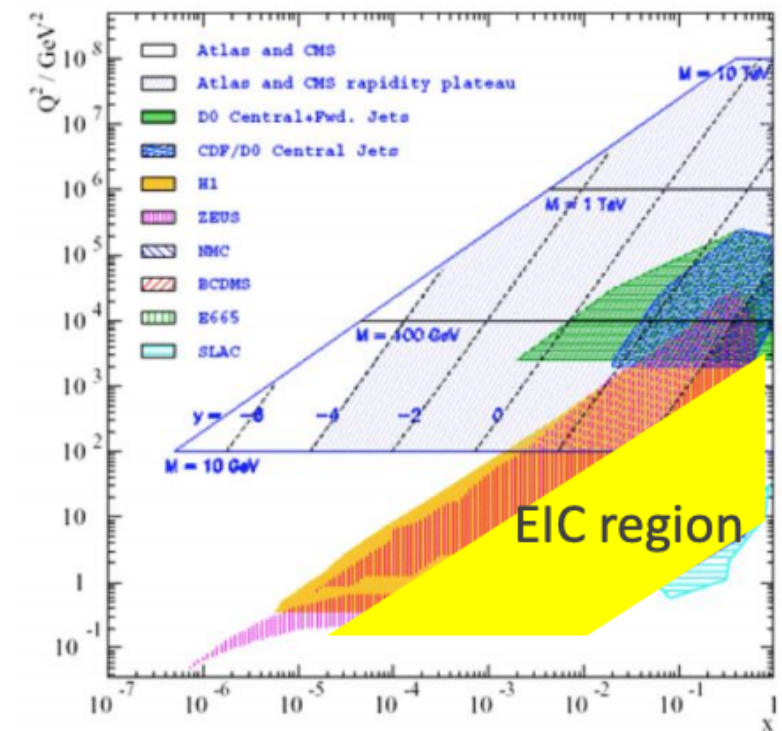


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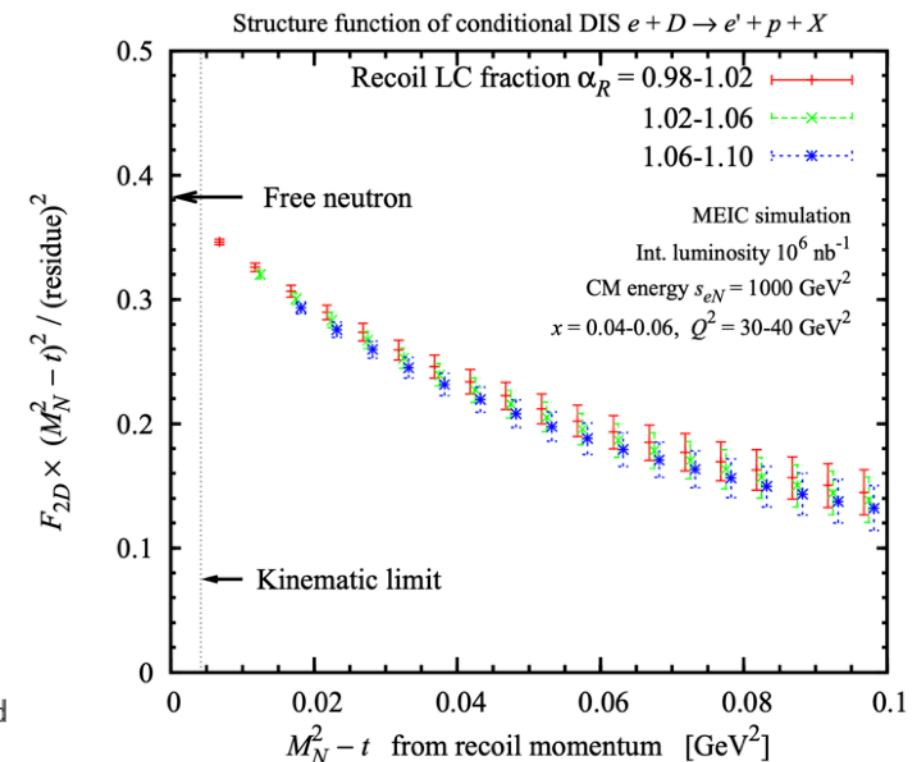


# Opportunities with EIC

- $F_1$ ,  $F_2$ ,  $F_L$  proton and deuteron
- High luminosity  $\rightarrow$  improve high  $x$  precision
- $F_2$  neutron with spectator tagging
- Impact studies with pseudo data show  $d$  quark precision significantly improved (comparable to current  $u$  precision)
- Also explore details of nuclear effects



— CJ15  
 — CJ15+F2p  
 — CJ15+F2p+F2ntag  
 — CJ15+F2p+F2ntag+F2d



A. Accardi et. al

W. Cosyn et al

EPJ Web Conf. 112 (2016) 01022



# Summary

- Structure functions contain information of internal structure of nucleons
- Large  $x$  region - large PDF uncertainties become a dominant systematic source for LHC physics
- Precise measurements of proton structure function
- Limited knowledge of neutron - lack of data, large uncertainty from nuclear effects
- Recent fixed target data and future program at JLab and EIC will provide significant constraints on neutron  $F_2$

**Thank you for your attention!**